

# **ADVANCED ARITHMETIC**

Published @ 2017 Trieste Publishing Pty Ltd

ISBN 9780649062324

Advanced Arithmetic by Charles E. Chadsey & Hubert M. Skinner

Except for use in any review, the reproduction or utilisation of this work in whole or in part in any form by any electronic, mechanical or other means, now known or hereafter invented, including xerography, photocopying and recording, or in any information storage or retrieval system, is forbidden without the permission of the publisher, Trieste Publishing Pty Ltd, PO Box 1576 Collingwood, Victoria 3066 Australia.

All rights reserved.

Edited by Trieste Publishing Pty Ltd.  
Cover @ 2017

This book is sold subject to the condition that it shall not, by way of trade or otherwise, be lent, re-sold, hired out, or otherwise circulated without the publisher's prior consent in any form or binding or cover other than that in which it is published and without a similar condition including this condition being imposed on the subsequent purchaser.

[www.triestepublishing.com](http://www.triestepublishing.com)

**CHARLES E. CHADSEY & HUBERT M. SKINNER**

# **ADVANCED ARITHMETIC**



ADVANCED  
ARITHMETIC

By

CHARLES E. CHADSEY, Ph.D.

SUPERINTENDENT OF SCHOOLS  
DETROIT, MICHIGAN

AND

HUBERT M. SKINNER, Ph.D.

AUTHOR OF  
"THE STORY OF THE LETTERS AND FIGURES"  
"THE SCHOOLMASTER IN LITERATURE"  
ETC.

ATKINSON, MENTZER & COMPANY  
CHICAGO NEW YORK BOSTON ATLANTA DALLAS

~~119.14.275~~  
Educ T 119.14.275  
✓ (III)

THE  
CHADSEY-SKINNER ARITHMETICS

THREE-BOOK SERIES

Elementary Arithmetic, XIV + 236 pages \$0.35  
Intermediate Arithmetic, VI + 256 pages .45  
Advanced Arithmetic, VI + 266 pages .55

TWO-BOOK SERIES

Elementary Arithmetic, XIV + 236 pages \$0.35  
Complete Arithmetic, VIII + 490 pages .65

Harvard Univ.  
Dept. of Education  
Library

JUL 23 1915

TRANSFERRED TO  
HARVARD COLLEGE LIBRARY  
1932

COPYRIGHT, 1914  
ATKINSON, MENTZER & COMPANY

## PREFACE

The work in Arithmetic in the upper elementary grades must accomplish two aims. It must retain or secure accuracy and reasonable rapidity in the mechanical manipulation of figures; and it must develop, so far as the maturity of the pupil and the time limits of the school program permit, the power to utilize the arithmetical processes presented in the solution of problems of the types that one may reasonably expect to find in ordinary life. These aims have been kept constantly in mind.

To eliminate the useless, the obsolete, and the unnecessarily technical and complex, and thus to secure sufficient opportunity for emphasis of the essential, is one of the commendable tendencies of the time. In the effort to accomplish this, and yet to retain what should be found in a standard arithmetic, which necessarily is frequently used for reference, topics are presented in the simplest manner consistent with clearness and accuracy.

The authors realize that the importance of certain topics varies in different localities and in different schools; and they suggest that where, for any reason, some topic is not deemed fundamentally necessary to secure the essential results desired, it may be treated as useful and interesting information, and need not be mastered in the thorough manner required in the case of other topics. It is believed, however, that no topics have been included that have not a legitimate place, or that do not deserve about the relative emphasis which is given in this series.

Where time problems are given as tests of readiness and quickness of work, as on pages 9, 12, 18 and 22, additional practice should be given to pupils who require more than average time for their solutions. Teachers are urged to devise tests revealing the relative ability of the pupils, and to supple-

ment the drill for the slower ones in such a way as to prevent unreasonable divergences in power at the end of the year's work. The time tests are inserted in order to call the attention of the teacher to this need for a careful observation of the powers and progress of the *individual pupil*.

The extended treatment accorded to the Metric System (which is in universal use throughout the world except among the English-speaking peoples) is deemed advisable at this time, because of our rapidly-growing intercourse with the American lands to the southward, and because of the claims which the science, as well as the commerce, of the great world makes upon it. Its nomenclature has been carried to the field of electricity and other sources of power, and may be expected to enter further fields of universal interest. There is no good reason why either the teaching or the study of this marvelously simple and interesting system should be dreaded or slighted as it has been in the past. The man or woman of to-day cannot afford to be ignorant of it, and youth is the proper time for its mastery.

For expert advice in the proportioning of the work, and its adaptation to specific grades, and for sedulous care in the arrangement of its parts, in supervising its make-up, acknowledgment is made to Mr. James C. Thomas, whose long and fruitful experience in school-book publishing qualifies him to be of the greatest service in all the innumerable details.

Credit is due to Mr. Charles L. Spain, Assistant Superintendent of the Detroit City Schools, for the valuable material supplied in the "Exercises for Practice" given on pages 251-266.

In the confident hope that we have combined, in their proper proportions, exercises to develop accuracy and facility in working with numbers, and topics of genuine value, with illustrative problems of a really practical nature, insuring the development of judgment on the part of the pupil, we present this advanced book of the series to the consideration of all interested in the teaching of the subject.

CHARLES E. CHADSEY  
HUBERT M. SKINNER

September, 1914



# CONTENTS

## PART I

	PAGES
REVIEW OF DEFINITIONS AND PRINCIPLES . . . . .	1-4
ADVANCED NUMERATION AND NOTATION . . . . .	5-8
Introduction of four new word elements— <i>deca</i> , <i>hecto</i> , <i>kilo</i> , and <i>myria</i> . Easy lessons in the application of Metric terms.	
ADVANCED WORK IN THE FUNDAMENTALS . . . . .	9-24
Time Problems in Addition; Adding of Long Columns; Time Problems in Subtraction; Substitutions in Subtraction; Making Change; Finding the Balance; The Multiplication Table up to and Including the 15's; Time Problems in Multiplication; Substitutions in Multiplication; Time Problems in Division; Relation of Multiplication to Division; Division by Factors.	
RATIO AND PROPORTION . . . . .	25-38
Antecedents and Consequents; Extremes and Means; Use of Cancellation in Proportion; Practice Work in Ratio and Proportion; Identical Ratios; Averages; Majorities and Pluralities.	
PERCENTAGE . . . . .	39-64
Review of Principles; Advanced Work in Percentage; Expense and Investment; Gross and Net Profits; Insurance—Fire, Marine, Casualty, Fidelity, Life, and Accident; Insurable Interest; Illustrative Problems; Taxes; Applications of Interest; Short Method of Interest; Exact Interest.	
BANKS AND BANKING . . . . .	65-90
National Banks; State Banks; Savings Banks; Trust Companies; Federal Reserve Banks; Deposits; Checks and Drafts; Monthly Statements; Loans and Bank Discount; Notes and Negotiable Paper; Partial Payments; Compound Interest; Rural Credits.	
MEASUREMENTS . . . . .	91-130
Review of Principles; Parallelograms; Squares; Triangles; Rhomboids; Trapezoids; Diamonds; Trapeziums; Diameter and Radius; Degrees; Angles; Protractors; Circles; Escribed Circles; Inscribed Circles; Pentagons; Hexagons; Octagons; Decagons; Prisms; Cylinders; Pyramids; Cones; Spheres; Cubes; Convex Areas; Applications of Long Measure; Applications of Square Measure; Applications of Cubic Measure.	

## VI

## CONTENTS

## PART II.

	PAGES
<b>REVIEW OF PRINCIPLES</b>	131-140
Foundation Work; Factoring; Practical Measurements; Fractions; Decimals and Cancellation; Per Cents; Interest, Discounts and Commissions; General Problems.	
<b>POWERS AND ROOTS</b>	141-160
Conventional Representations; Involution; Evolution; Perfect Squares; Tables of Square Roots of Numbers; Applications of Square Roots; Applications of Cube Roots; Tables of Cube Roots of Numbers; Roots of Fractions; General Problems in Evolution; Extraction of Square Roots; Practice Problems.	
<b>STOCKS AND BONDS</b>	161-174
Common and Preferred Stocks; Stock Certificates; Practice Problems; Special Illustrative Problems; National, State, County, and Corporation Bonds; Comparison of Stocks and Bonds, Signatures and Seals; Bonds and Coupons; Practice Problems; Partnerships; Domestic Exchange; Foreign Exchange; Travelers' Checks.	
<b>MONEY OF OTHER LANDS</b>	175-182
English Money; Other Monetary Systems; Problems Relating to Monetary Units of Equal Value; Problems relating to Monetary Units of Different Values.	
<b>LONGITUDE AND TIME</b>	183-194
Longitude and "Length"; Meridians; Latitude and Parallels; Longitude and Time; International Date Line; Standard Time.	
<b>THE METRIC SYSTEM</b>	195-210
Historical Statement; Basis of the Metric System; Growing Importance of the Metric System; Illustrative Problems; New Word Elements; Metric Long Measure; Practice with the Decimeter; Metric Square Measure; Metric Cubic Measure; Multiplication and Division Tables; Metric Dry and Liquid Measure; Metric Weight; Familiar Commercial Denominations.	
<b>MISCELLANEOUS WORK</b>	211-218
Direct and Inverse Proportion; Present Worth; Experience Problems; Temperature; Weather Forecast; Thermometers and Barometers; Class Exercises; Practical Weather Problems; Approximation Problems.	
<b>SUPPLEMENT</b>	219-250
Vocational Problems—Dairying, Poultry, Bee Culture, Foods, Horticulture, Lumbering, Coal and Oil, Mechanics, Electricity, Construction Work, Good Roads, Transportation and Travel; Illustrated Tables of Denominate Numbers and Metric Measurements; Tables of Food Compositions; Legal Weights; Foreign Money Values, and Areas and Populations; Spanish American Land Measure; Perpetual Calendar and Explanatory Problems.	
<b>EXERCISES FOR PRACTICE</b>	251-266

# Advanced Arithmetic

---

## PART I

	PAGES
DEFINITIONS AND PRINCIPLES . . . . .	1 to 4
Review of Elementary Processes.	
ADVANCED NUMERATION AND NOTATION . . . . .	5 to 8
Introducing four New Word Elements.	
ADVANCED WORK IN FUNDAMENTALS . . . . .	9 to 24
Addition, Subtraction, Multiplication, and Division.	
RATIO AND PROPORTION . . . . .	25 to 38
Antecedents, Consequents, Means, Extremes, and Averages.	
PERCENTAGE . . . . .	39 to 64
Taxation, Insurance, Banking, Negotiable Paper.	
BANKS AND BANKING . . . . .	65 to 90
National, State, Savings, and Federal Reserve Banks.	
MEASUREMENTS . . . . .	91 to 130

### REVIEW OF DEFINITIONS AND PRINCIPLES

Numeration is reading numbers written in figures.

Notation is writing numbers in figures.

Arabic figures consist of nine *digits* (taking their name from the fingers of the human hand) and the cipher, which is used to fill vacant places in written numbers. There is no figure to represent the tenth digit, or unit.

When this is reached the circuit of units is complete, and this circuit is called a *ten*, and written in the next *order*, or place of figures.

A full period consists of three orders, numbered from the right. The first order is *units*; the second, *tens*; the third, *hundreds*.